How far can the field go?

# penetration depth, London equations





Fritz London



Lecture 3: April 18, 2024

by Alexander Tsirlin, Leipzig University

Superconductivity I, SS 24 How far can the field go?

#### London gauge





Standard track gauge 1435 mm

Image credit: SPSmiler (public domain)

#### London gauge





Standard track gauge 1435 mm

#### London gauge will be our standard gauge for now

Image credit: SPSmiler (public domain)

Superconductivity I, SS 24 How far can the field go?



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# Personality Fritz London

Superconductivity I, SS 24 How far can the field go?

- 1921: PhD in philosophy
- 1922–24 gymnasium science teacher
- 1927-33: Schrödinger's assistant in Berlin
- 1927: theory of chemical bond (Heitler-London scheme)
- 1930: theory of molecular interactions (London force)



Physics colloquium next week

#### Tuesday, 23 Apr 2024 at 16:30

#### **Dr. Alexander Blum**

MPI Wissenschaftsgeschichte Berlin

Matrices vs. wave functions: Schrödinger's notebooks and his equivalence proof

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- 1922–24 gymnasium science teacher
- 1927–33 Schrödinger's assistant in Berlin
- 1927: theory of chemical bond (Heitler-London scheme)
- 1930: theory of molecular interactions (London force)
- 1933: emigrates to England (Oxford) together with his younger brother Heinz
- 1935: London equations



#### London brothers



Heinz London 1907–1970

experiment



Fritz London 1900–1954

theory

- 1927: theory of chemical bond (Heitler-London scheme)
- 1930: theory of molecular interactions (London force)
- 1935: London equations
- 1936 moves to Paris
- from 1936: superfluidity and superconductivity
- from 1939: professor at Duke University, North Carolina, US
- 1950: influential book Superfluids



- 1927: theory of chemical bond (Heitler-London scheme)
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- 1935 London equations
- 1936 moves to Paris
- from 1936: superfluidity and superconductivity
- from 1939: professor at Duke University, North Carolina, US
- 1950: influential book Superfluids

"The fact that in 15 years London has not seen fit to make any substantial alterations to the fundamental framework of his theory is to be regarded not as evidence of a conservative nature, but as testimony to the logical beauty of the theory in its original form"

Brian Pippard



#### Penetration depth



### Penetration depth



#### Penetration depth from dc-susceptibility



With  $d\ll\lambda_L$ , the susceptibility goes below the Meissner limit



particle size decreases

D. Shoenberg, Proc. Royal Soc. 175, 49 (1940)



## Experiment

flux quantization

### Continuity of the phase







#### phase is continuous 🖌

Image credit: Supra 2011 (fair use)

#### Measurement of flux quantization



#### Flux quantization: When magnetism climbs stairs



Both experiments consistently indicated  $\Phi_0 = \pi \hbar/e$ 

Image credit: Gross and Marx, Festkörperphysik

Macroscopic manifestation of a quantum state

#### Microscopic: quantum nature of the superconducting state phase coherence

Macroscopic: measurable effect for the magnetic flux

# **Thinking big**

Fritz London's single-minded thinking led him to surpass even Einstein, as he believed correctly that quantum mechanics was right at all scales, including the macroscopic.

Nature 437, 625 (2005)

Macroscopic manifestation of a quantum state

#### Microscopic: quantum nature of the superconducting state phase coherence

Macroscopic: measurable effect for the magnetic flux

# **Thinking big**

Fritz London's single-minded thinking led him to surpass even Einstein, as he believed correctly that quantum mechanics was right at all scales, including the macroscopic.

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Supercurrent is related to the gradient of phase, abla heta